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Science **314**, 1430 (2006);

DOI: 10.1126/science.1133732

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Optical Atomic Coherence at the 1-Second Time Scale

Martin M. Boyd, Tanya Zelevinsky, Andrew D. Ludlow, Seth M. Foreman, Sebastian Blatt, Tetsuya Ido,* Jun Ye†

Highest-resolution laser spectroscopy has generally been limited to single trapped ion systems because of the rapid decoherence that plagues neutral atom ensembles. Precision spectroscopy of ultracold neutral atoms confined in a trapping potential now shows superior optical coherence without any deleterious effects from motional degrees of freedom, revealing optical resonance linewidths at the hertz level with a good signal-to-noise ratio. The resonance quality factor of 2.4×10^{14} is the highest ever recovered in any form of coherent spectroscopy. The spectral resolution permits direct observation of the breaking of nuclear spin degeneracy for the 1S_0 and 3P_0 optical clock states of ^{87}Sr under a small magnetic bias field. This optical approach for excitation of nuclear spin states allows an accurate measurement of the differential Landé g factor between 1S_0 and 3P_0 . The optical atomic coherence demonstrated for collective excitation of a large number of atoms will have a strong impact on quantum measurement and precision frequency metrology.

The relative rates of coherent interaction and decoherence in a quantum system are of fundamental importance for both quantum information science (1) and precision metrology (2). Enhancing their ratio, which is equivalent to improving spectral resolving power, characterizes much of the recent progress in these fields. Trapped ions have so far provided the best platform for research in this direction, resulting in a number of seminal achievements (3–8). The principal advantage of the ion system lies in the clean separation between the internal atomic state and the external center-of-mass motion, leading to long coherence times associated with both internal and external degrees of freedom. A large ensemble of neutral atoms offers obvious benefits in the signal size and scalability of a quantum system (9, 10). Multi-atom collective effects can also dramatically enhance the coherent matter/field interaction strength (11). However, systems based on neutral atoms normally suffer from decoherence resulting from coupling between their internal and external degrees of freedom (12). In this article, we report a record-level spectral resolution in the optical domain based on a doubly forbidden transition in neutral atomic strontium. The atoms are confined in an optical trapping potential engineered for accurate separation between these degrees of freedom (13). The large number of quantum absorbers provides a dramatic enhancement in signal size for the recovered hertz-linewidth optical resonance profile.

The demonstrated neutral-atom coherence properties will affect a number of research fields, with some initial results reported here. Optical

atomic clocks (14) benefit directly from the enhanced signal size and the high resonance quality factor Q . Tests of atomic theory can be performed with increased precision. The available spectral resolution also enables a direct optical manipulation of nuclear spins that are decoupled from the electronic angular momentum. Nuclear spins can have an exceedingly long relaxation time, making them a valuable alternative for quantum information processing and storage. Two ground-state nuclear spins can, for example, be entangled through dipolar interactions when photoassociation channels to high-lying electronic states (such as 3P_1) are excited (15). Combined with a quantum degenerate gas, the enhanced precision in measurement will further strengthen the prospects of using optical lattices to engineer condensed matter systems (for example, allowing massively parallel quantum measurements).

Much of the recent interest in alkaline earth atoms (and similar atoms and ions, such as Yb, Hg, In^+ , and Al^+) arises from the study of the forbidden optical transitions, both for metrological applications and as a means for quantum control, with an important achievement being highly effective narrow line laser cooling (16–18). The spin-forbidden 1S_0 - 3P_1 transition has been extensively studied as a potential optical frequency standard in Mg (19), Ca (20), and Sr (21, 22) and has recently been explored as a tool for high-resolution molecular spectroscopy through photoassociation in ultracold Sr (15). The doubly forbidden 1S_0 - 3P_0 transition is weakly allowed as a result of hyperfine-induced state mixing, yielding a linewidth of ~ 1 mHz for ^{87}Sr with a nuclear spin of $\frac{1}{2}$. This transition is a particularly attractive candidate for optical domain experiments, where long coherence times are desirable, and is currently being aggressively pursued for the realization of an optical atomic clock (23–26). Furthermore, because of the lack of electronic angular momentum, the level shifts of the two states can be matched with high accuracy in an

optical trap (13), such that external motions do not decohere the superposition of the two states. Using optically cooled ^{87}Sr atoms in a zero-differential-Stark shift one-dimensional (1D) optical lattice and a cavity-stabilized probe laser with a sub-hertz spectral width, we have achieved probe-time-limited resonance linewidths of 1.8 Hz at the optical carrier frequency of 4.3×10^{14} Hz. The ratio of these frequencies, corresponding to a $Q \approx 2.4 \times 10^{14}$, is the highest obtained for any coherent spectral feature.

This ultrahigh spectral resolution allows us to perform experiments in the optical domain analogous to radio-frequency nuclear magnetic resonance (NMR) studies. Under a small magnetic bias field, we make direct observations of the magnetic sublevels associated with the nuclear spin. Furthermore, we have precisely determined the differential Landé g factor between 1S_0 and 3P_0 that arises from hyperfine mixing of 3P_0 with 3P_1 and 1P_1 . This optical measurement approach uses only a small magnetic bias field, whereas traditional NMR experiments performed on a single state (either 1S_0 or 3P_0) would need large magnetic fields to induce splitting in the radio frequency range. Because the state mixing between 3P_0 , 3P_1 , and 1P_1 arises from both hyperfine interactions and external fields, the use of a small field permits an accurate, unperturbed measurement of mixing effects. Optical manipulation of nuclear spins shielded by two spin-paired valence electrons, performed with a superior spatial and atomic state selectivity, may provide an attractive choice for quantum information science.

Optical atomic clocks based on neutral atoms benefit directly from a large signal-to-noise ratio (S/N) and a superior line Q . Resolving nuclear sublevels with optical spectroscopy permits improved measurements of systematic errors associated with the nuclear spin, such as linear Zeeman shifts, and tensor polarizability that manifests itself as nuclear spin-dependent trap polarization sensitivity. Tensor polarizability of the 3P_0 state is one of the important potential systematic uncertainties for fermion-based clocks and is one of the primary motivations for recent proposals involving electromagnetically induced transparency resonances or dc magnetic field-induced state mixing in bosonic isotopes (27–29). The work reported here has permitted control of these systematic effects to $\sim 5 \times 10^{-16}$ (30). Given the superior S/N from the large number of quantum absorbers, we expect this system to be competitive among the best performing clocks in terms of stability. Accuracy is already approaching the level of the best atomic fountain clocks (31, 32), and absolute frequency measurement is limited by the Cs clock-calibrated maser signal available to us by means of a fiber link (33). An all-optical clock comparison is necessary to reveal its greater potential.

To fully exploit the ultranarrow hyperfine-induced transition for high-precision spectroscopy

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py, it is critical to minimize decoherence from both fundamental and technical origins. The ~ 100 -s coherence time available from the ^{87}Sr atoms is not yet experimentally practical as a result of environmental perturbations to the probe laser phase at long time scales, but atomic coherence in the optical domain at 1 s can already greatly improve the current optical clock and quantum measurements. To achieve long atomic coherence times, we trap atoms in an optical lattice with a zero net ac Stark shift between the two clock states, enabling a large number of neutral atoms to be interrogated free of perturbations. The tight atomic confinement enables long probing times and permits spectroscopy free of broadening by atomic motion and photon recoil.

For the highest spectral resolution, it is necessary for the probe laser to have a narrow intrinsic linewidth and a stable center frequency. A cavity-stabilized 698-nm diode laser is used as the optical local oscillator for $^1\text{S}_0$ - $^3\text{P}_0$ spectroscopy (34). The linewidth of this oscillator has been characterized by comparison with a second laser operating at 1064 nm via an optical frequency comb linking the two distant colors. A heterodyne optical beat signal between the two lasers, measured by the frequency comb, reveals a laser linewidth of <0.3 Hz (resolution-bandwidth-limited) at 1064 nm for a 3-s integration time. This result demonstrates the ability of the frequency comb to transfer optical phase coherence (~ 1 rad/s) across hundreds of terahertz. Our frequency comb is also referenced to a hydrogen maser calibrated by the National Institute of Standards and Technology (NIST) F1 Cs fountain clock (31), which allows us to accurately measure the probe laser frequency to 3×10^{-13} at 1 s. Additionally, the 698-nm laser has been compared with an independent laser system operating at the same wavelength, revealing a resolution-bandwidth-limited laser linewidth of 0.2 Hz, which increases to ~ 2 Hz for a 30-s integration time. After removing the linear drift, the stability of this local oscillator is $\sim 1 \times 10^{-15}$ from 1 to 1000 s, which is limited by the thermal noise of the cavity mirrors. Thus, the probe laser provides the optical coherence needed to perform experiments at the 1-s time scale.

^{87}Sr atoms are captured from an atomic beam and cooled to 1 mK by means of a magneto-optical trap (MOT) acting on the strong $^1\text{S}_0$ - $^1\text{P}_1$ transition (Fig. 1A). This step is followed by a second-stage MOT with the use of the narrow $^1\text{S}_0$ - $^3\text{P}_1$ intercombination line that cools the atoms to ~ 1.5 μK . During narrow line cooling, a nearly vertical 1D lattice is overlapped with the atom cloud for simultaneous cooling and trapping. The lattice is generated by a ~ 300 -mW standing wave with a 60- μm beam waist at the wavelength of 813.428(1) nm, where the $^1\text{S}_0$ and $^3\text{P}_0$ ac Stark shifts from the trapping field are equal (35). The cooling and loading stages take ~ 0.7 s and result in a sample of 10^4 atoms,

spread among ~ 100 lattice sites. The vacuum-limited lattice lifetime is >1 s. The atoms are confined in the Lamb-Dicke regime along the axis of the optical lattice. The Lamb-Dicke parameter, or the square root of the ratio of recoil frequency to trap oscillation frequency, is ~ 0.3 . Both the axial and radial trap frequencies are much larger than the $^1\text{S}_0$ - $^3\text{P}_0$ transition linewidth, leading to the spectral feature composed of a sharp optical carrier and two sets of resolved motional sidebands. One pair of sidebands is observed ± 40 kHz away from the carrier, corresponding to the axial oscillation frequency in the lattice. The red-detuned sideband is strongly suppressed, indicating that nearly all atoms are in the motional ground state along the lattice axis. The second pair of sidebands at ± 125 Hz from the carrier, with

nearly equal amplitudes, corresponds to the trap oscillation frequency in the transverse plane.

With atoms confined in the lattice, the linearly polarized (parallel to the lattice polarization) 698-nm laser drives the π transitions (Fig. 1B) for probe times between 0.08 and 1 s, depending on the desired spectral resolution limited by the Fourier transform of the probe time. The effect of the probe laser is detected in two ways. First, after some atoms are excited to the long-lived $^3\text{P}_0$ state by the probe laser, the remaining $^1\text{S}_0$ population is measured by exciting the strong $^1\text{S}_0$ - $^1\text{P}_1$ transition with a resonant pulse at 461 nm. The $^1\text{S}_0$ - $^1\text{P}_1$ pulse scatters a large number of signal photons and heats the $^1\text{S}_0$ atoms out of the lattice, leaving only the $^3\text{P}_0$ atoms. Once the $^1\text{S}_0$ atoms have been removed, the $^3\text{P}_0$ population is determined by driving the $^3\text{P}_0$ - $^3\text{S}_1$ and $^3\text{P}_2$ - $^3\text{S}_1$

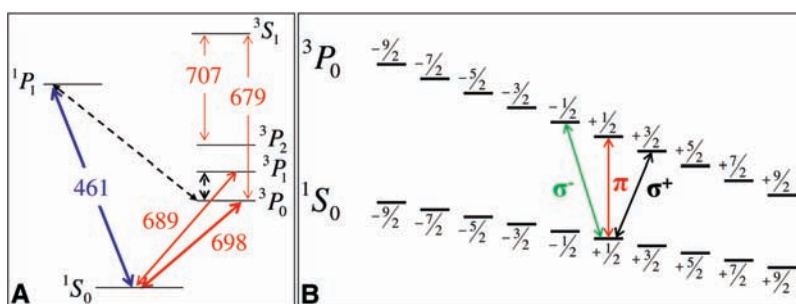
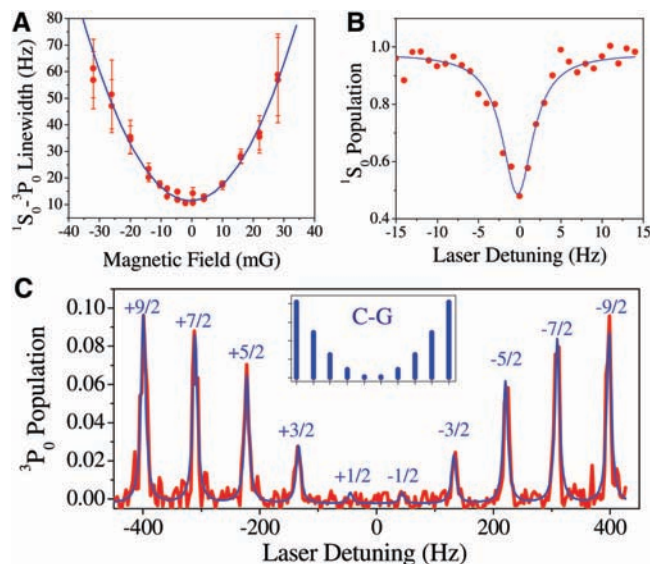


Fig. 1. (A) Partial ^{87}Sr energy-level diagram. Solid arrows show relevant electric dipole transitions with wavelengths in nanometers. Dashed arrows show the hyperfine interaction-induced state mixing between $^3\text{P}_0$ and $^3\text{P}_1$ and between $^3\text{P}_0$ and $^1\text{P}_1$, which provides the nonzero electric dipole moment for the doubly forbidden 698-nm transition. (B) The mixing alters the Landé g factor of the $^3\text{P}_0$ state such that it is $\sim 50\%$ larger than that of $^1\text{S}_0$, resulting in a linear Zeeman shift for the $^1\text{S}_0$ - $^3\text{P}_0$ transition in the presence of a small magnetic field. The large nuclear spin of ^{87}Sr ($I = 7/2$) results in 10 sublevels for the $^1\text{S}_0$ and $^3\text{P}_0$ states, providing 28 possible transitions from the ground state.

Fig. 2. Spectroscopy of the $^1\text{S}_0$ - $^3\text{P}_0$ transition in ^{87}Sr . A pair of Helmholtz coils provides a variable field along the lattice (and probe) polarization axis, allowing a measurement of the field-dependent transition linewidth as shown in (A) where an 80-ms interrogation pulse is used, limiting the width to ~ 10 Hz. Error bars in (A) indicate measurement uncertainty in linewidth. (B) A representative spectrum when the ambient field is well controlled. Here, a longer probe time is used (~ 480 ms or a 1.8-Hz Fourier limit) but the linewidth is limited to 4.5 Hz by residual magnetic fields and possibly residual Stark shifts. (C) A field of 0.77 G is applied along the polarization axis, and the individual Fourier-limited (10 Hz) π transitions are easily resolved. Data are shown in red, and a fit of 10 evenly spaced transitions is shown in blue. The calculated transition probabilities based on Clebsch-Gordan (C-G) coefficients are included in the inset. In (B) and (C), the population is scaled by the total number of atoms available for spectroscopy ($\sim 10^4$).



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transitions (Fig. 1A), resulting in atomic decay to the ground state via 3P_1 for a second measurement with the use of the 1S_0 - 1P_1 pulse. The second measurement provides superior S/N because only atoms initially excited by the 698-nm probe laser contribute to the fluorescence signal, and the zero background is not affected by shot-to-shot atom number fluctuations. Combining both approaches permits signal normalization against atom number fluctuations.

Although the 3P_0 and 1S_0 states are magnetically insensitive to first order, the hyperfine-induced state mixing, which allows the otherwise forbidden transition, modifies the 3P_0 nuclear g factor by $\sim 50\%$. This effect results in a linear Zeeman shift in the 1S_0 - 3P_0 transition of about -100 Hz/G per magnetic sublevel m_F (36, 37), where we use the convention that the g factor and nuclear magnetic moment carry the same sign and $1\text{ G} = 10^{-4}\text{ T}$. This effect is shown schematically in Fig. 1B, where the 10 nuclear spin sublevels are resolved for the 1S_0 and 3P_0 states in the presence of a magnetic field. The linear Zeeman shift is an important issue for high-resolution spectroscopy, because the magnetic sensitivity can cause undesirable broadening of the transition, as well as line center shifts due to unbalanced population distribution among the sublevels. To achieve the narrowest resonance, the ambient magnetic field must be compensated with three orthogonal sets of Helmholtz coils. An example of this zeroing process is shown in Fig. 2A, where the transition linewidths are measured under various field strengths. After zeroing the field, narrow resonances as in Fig. 2B are routinely obtained. The displayed transition linewidth of 4.5 Hz [full width at half maximum (FWHM)] represents a resonance Q of $\sim 10^{14}$. The good S/N for the narrow line resonance achieved without any averaging or normalization arises from the contribution of 10^4 atoms. The

ultrahigh spectral resolution has allowed a recent measurement of systematic effects for the optical clock transition at the 9×10^{-16} level (30).

The high-resolution spectroscopy enables direct measurement of the differential Landé g factor (Δg) between 3P_0 and 1S_0 . To observe this state mixing effect, we applied a small magnetic field ($<1\text{ G}$) along the direction of the lattice polarization, and the probe laser polarization was again fixed along this quantization axis to drive π transitions. Figure 2C shows a direct observation of the hyperfine-induced state mixing in the form of 10 resolved transition components, with their relative amplitudes influenced by the Clebsch-Gordan coefficients. The narrow linewidth of the forbidden transition allows this nuclear-magnetic-resonance-like g -factor experiment to be performed optically at small magnetic fields. The magnitude of Δg can be measured by mapping out the line splitting versus magnetic field. Alternatively, 18 σ^+ and σ^- transitions (Fig. 1B) can be used to extract both the magnitude and sign [relative to the known 1S_0 g factor (38)] of Δg , without accurate calibration of the field. Using the latter approach, we find $\Delta g = -108.8(4)$ Hz/G per m_F . The measured Δg permits determination of the 3P_0 lifetime of 140(40) s, in agreement with recent ab initio calculations (39, 40). The uncertainty is largely dominated by inconsistencies among hyperfine mixing models (36, 37).

The linewidth of each spectral feature in Fig. 2C is Fourier-limited by the 80-ms probe time to ~ 10 Hz. With the nuclear spin degeneracy removed by a small magnetic field, individual transition components allow exploration of the ultimate limit of our spectral resolution by eliminating any broadening mechanisms due to residual magnetic fields or light shifts, the likely limitation for data such as in Fig. 2B. To reduce the Fourier limit for the linewidth, we

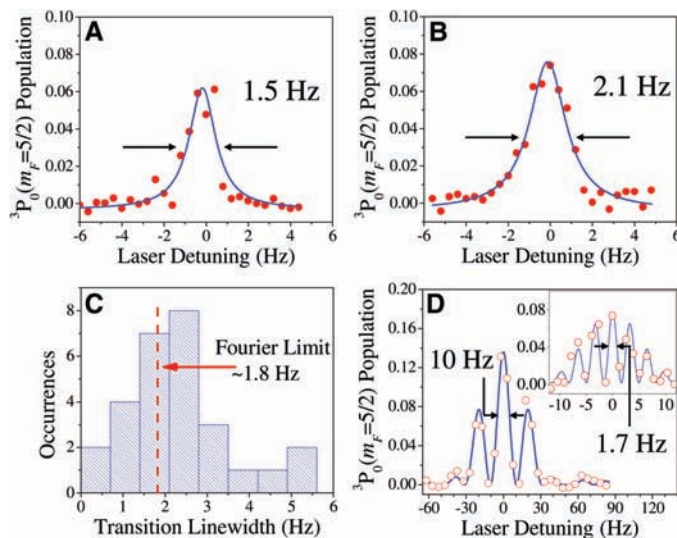
probed the spectra of a single resolved sublevel ($m_F = 5/2$ in this case) using π polarization with the time window extended to 480 ms. Figure 3, A and B, shows some sample spectra of the isolated 1S_0 ($m_F = 5/2$)- 3P_0 ($m_F = 5/2$) transition with a Fourier-limited linewidth of 1.8 Hz, representing a line Q of $\sim 2.4 \times 10^{14}$. This Q is reproduced reliably, as evidenced by the histogram of linewidths measured in the course of 1 hour (Fig. 3C). Typical linewidths are ~ 1 to 3 Hz, with the statistical scatter owing to residual probe laser noise at the 10-s time scale.

To further explore the limit of coherent atom-light interactions, we have also performed two-pulse optical Ramsey experiments on an isolated π transition. When a system is lifetime-limited, the Ramsey technique can achieve higher spectral resolution at the expense of S/N , leading to useful information on the decoherence process. By performing the experiment in the lattice, the Ramsey interrogation pulse can be prolonged, resulting in a markedly reduced Rabi pedestal width as compared to free-space spectroscopy. The reduced number of fringes greatly simplifies identification of the central fringe for applications such as frequency metrology. The fringe period (in Hz) is determined by the sum of the pulse interrogation time τ_R and the free-evolution time between pulses T_R and is given by $1/(\tau_R + T_R)$. Figure 3D shows a sample Ramsey spectrum, where $\tau_R = 20$ ms and $T_R = 25$ ms, yielding a fringe pattern with a period of 20.8(3) Hz and fringe FWHM 10.4(2) Hz. For the same transition with τ_R raised to 80 ms and T_R to 200 ms (Fig. 3D, inset), the width of the Rabi pedestal is reduced to ~ 10 Hz, and the recorded fringe linewidth is 1.7(1) Hz.

This linewidth is recovered without substantial degradation of the fringe signal size, suggesting that the spectral resolution is limited by phase decoherence between light and atoms and not by effects such as trap lifetime. A limit of 1 to 2 Hz is consistent with our measurements of the probe laser noise integrated over the time scales used for spectroscopy. Other potential limitations to the spectral width include Doppler broadening resulting from the relative motion between the lattice and probe beams and broadening as a result of tunneling in the lattice. Future measurements will be improved by locking the probe laser to one of the resolved nuclear spin transitions to further suppress residual laser fluctuations. Although the S/N associated with a sublevel resonance is reduced when compared to a measurement involving all degenerate sublevels, $>10^3$ atoms still contribute to the signal, which allows measurement to proceed without averaging. Clearly, reaching the atom shot-noise limit and performing quantum state preparations will further enhance the S/N .

The line Q of $\sim 2.4 \times 10^{14}$ achieved here provides practical improvements in the fields of precision spectroscopy and quantum measurement. The neutral atom-based spectroscopic system now parallels the best ion systems in

Fig. 3. Spectroscopy of the isolated 1S_0 ($m_F = 5/2$)- 3P_0 ($m_F = 5/2$) transition. Resolving individual sublevels allows spectroscopy without magnetic or Stark broadening. Spectra in (A) and (B) are taken under identical experimental conditions by means of a pulse time of 480 ms, and linewidths of 1.5(2) and 2.1(2) Hz are achieved. (C) A histogram of the linewidths of 28 traces obtained within ~ 1 hour. The average linewidth is near the 1.8-Hz Fourier limit (dashed red line). (D) Ramsey fringes with a 20.8(3)-Hz period and 10.4(2)-Hz fringe width, with data shown as open circles. Inset shows a Ramsey pattern with a 1.7(1)-Hz fringe FWHM.



terms of fractional resolution but greatly surpasses the latter in signal size. For optical frequency standards, the high resolution presented here has improved studies of systematic errors for the evaluation of clock accuracy. With these narrow resonances, clock instability below 10^{-16} at 100 s is anticipated in the near future. For quantum physics and engineering, this system opens the door to using neutral atoms for experiments in which long coherence times are necessary, motional and internal atomic quantum states must be controlled independently, and many parallel processors are desired.

References and Notes

- D. Leibfried, R. Blatt, C. Monroe, D. Wineland, *Rev. Mod. Phys.* **75**, 281 (2003).
- R. J. Rafac *et al.*, *Phys. Rev. Lett.* **85**, 2462 (2000).
- P. O. Schmidt *et al.*, *Science* **309**, 749 (2005).
- H. Häffner *et al.*, *Phys. Rev. Lett.* **90**, 143602 (2003).
- H. Häffner *et al.*, *Nature* **438**, 643 (2005).
- H. S. Margolis *et al.*, *Science* **306**, 1355 (2004).
- T. Schneider, E. Peik, C. Tamm, *Phys. Rev. Lett.* **94**, 230801 (2005).
- P. Dubé *et al.*, *Phys. Rev. Lett.* **95**, 033001 (2005).
- D. L. Haycock, P. M. Alsing, I. H. Deutsch, J. Grondalski, P. S. Jessen, *Phys. Rev. Lett.* **85**, 3365 (2000).
- I. Bloch, M. Greiner, in *Advances in Atomic Molecular and Optical Physics* (Academic Press, San Diego, CA, 2005), vol. 52, pp. 1–47.
- A. T. Black, H. W. Chan, V. Vuletic, *Phys. Rev. Lett.* **91**, 203001 (2003).
- J. Ye, D. W. Vernooy, H. J. Kimble, *Phys. Rev. Lett.* **83**, 4987 (1999).
- H. Katori, M. Takamoto, V. G. Pal'chikov, V. D. Ovsinnikov, *Phys. Rev. Lett.* **91**, 173005 (2003).
- See, for example, *Science* **306**, no. 5700 (2004).
- T. Zelevinsky *et al.*, *Phys. Rev. Lett.* **96**, 203201 (2006).
- T. Mukaiyama, H. Katori, T. Ido, Y. Li, M. Kuwata-Gonokami, *Phys. Rev. Lett.* **90**, 113002 (2003).
- T. H. Loftus, T. Ido, A. D. Ludlow, M. M. Boyd, J. Ye, *Phys. Rev. Lett.* **93**, 073003 (2004).
- T. H. Loftus, T. Ido, M. M. Boyd, A. D. Ludlow, J. Ye, *Phys. Rev. A* **70**, 063413 (2004).
- F. Ruschewitz *et al.*, *Phys. Rev. Lett.* **80**, 3173 (1998).
- U. Sterr *et al.*, *C. R. Phys.* **5**, 845 (2004).
- T. Ido *et al.*, *Phys. Rev. Lett.* **94**, 153001 (2005).
- G. Ferrari *et al.*, *Phys. Rev. Lett.* **91**, 243002 (2003).
- I. Courtillot *et al.*, *Phys. Rev. A* **68**, 030501 (2003).
- M. Takamoto, F. L. Hong, R. Higashi, H. Katori, *Nature* **435**, 321 (2005).
- A. D. Ludlow *et al.*, *Phys. Rev. Lett.* **96**, 033003 (2006).
- R. Le Targat, *Phys. Rev. Lett.* **97**, 130801 (2006).
- R. Santra, E. Arimondo, T. Ido, C. H. Greene, J. Ye, *Phys. Rev. Lett.* **94**, 173002 (2005).
- T. Hong, C. Cramer, W. Nagourney, E. N. Fortson, *Phys. Rev. Lett.* **94**, 050801 (2005).
- Z. W. Barber *et al.*, *Phys. Rev. Lett.* **96**, 083002 (2006).
- The magnetic field-induced frequency uncertainty is determined from the product of the measured residual magnetic field by means of the clock transition linewidth and experimentally determined frequency shifts versus given magnetic fields along three orthogonal directions. The total systematic uncertainty includes Stark shifts associated with the lattice and the probe beams, magnetic shift, density shift, and blackbody shift. For further details, see M. M. Boyd *et al.*; preprint available at http://arxiv.org/PS_cache/physics/pdf/0611/0611067.pdf.
- T. P. Heavner, S. R. Jefferts, E. A. Donley, J. H. Shirley, T. E. Parker, *Metrologia* **42**, 411 (2005).
- S. Bize *et al.*, *J. Phys. B Atom. Mol. Opt. Phys.* **38**, S449 (2005).
- J. Ye *et al.*, *J. Opt. Soc. Am. B* **20**, 1459 (2003).
- A. D. Ludlow *et al.*; preprint available at <http://arxiv.org/ftp/physics/papers/0610/0610274.pdf>.
- A. Brusch, R. Le Targat, X. Baillard, M. Fouché, P. Lemonde, *Phys. Rev. Lett.* **96**, 103003 (2006).
- H. J. Kluge, H. Sauter, *Z. Phys.* **270**, 295 (1974).
- A. Lurio, M. Mandel, R. Novick, *Phys. Rev.* **126**, 1758 (1962).
- L. Olschewski, *Z. Phys. A* **249**, 205 (1972).
- S. G. Porsev, A. Derevianko, *Phys. Rev. A* **69**, 042506 (2004).
- R. Santra, K. V. Christ, C. H. Greene, *Phys. Rev. A* **69**, 042510 (2004).
- We thank T. Parker and S. Diddams for providing the NIST hydrogen maser signal; J. C. Bergquist, I. H. Deutsch, C. H. Greene, J. L. Hall, and P. Julienne for helpful discussions; and X. Huang for technical assistance. The work at JILA is supported by the Office of Naval Research, NIST, and NSF. A.D.L. is supported by NSF–Interdisciplinary Graduate Education, Research and Training and the University of Colorado Optical Science and Engineering Program. T.Z. is a National Research Council postdoctoral fellow. T.I. acknowledges support from the Japan Science and Technology Agency.

10 August 2006; accepted 18 October 2006
10.1126/science.1133732

Macroscopic Hierarchical Surface Patterning of Porphyrin Trimers via Self-Assembly and Dewetting

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The use of bottom-up approaches to construct patterned surfaces for technological applications is appealing, but to date is applicable to only relatively small areas (~10 square micrometers). We constructed highly periodic patterns at macroscopic length scales, in the range of square millimeters, by combining self-assembly of disk-like porphyrin dyes with physical dewetting phenomena. The patterns consisted of equidistant 5-nanometer-wide lines spaced 0.5 to 1 micrometers apart, forming single porphyrin stacks containing millions of molecules, and were formed spontaneously upon drop-casting a solution of the molecules onto a mica surface. On glass, thicker lines are formed, which can be used to align liquid crystals in large domains of square millimeter size.

The formation of complex submicrometer patterns on surfaces that extend over macroscopic distances underlies the fabrication of integrated circuits and microelectromechanical devices (1–3). However, for many

applications, such as detection arrays and optical elements, well-defined symmetrical patterns can be exploited, especially if the methods decrease the number of processing steps needed or avoid surface-invasive steps that scratch, rub, or etch the surface. Examples of complex pattern formation by noninvasive techniques are still few, usually require large polymeric molecules, and are often of small spatial extent (4–12). Self-assembly of molecules on a surface can be a simple, versatile, and less time-consuming approach and may lead to defect-free structures

(1), especially if combined with physical processes such as dewetting and contact-line pinning. Here we report the spontaneous formation of periodic patterns of exceptionally long (up to 1 mm) columnar stacks of porphyrin dye molecules at a solid/liquid interface, with highly defined spatial and parallel ordering. These self-assembled patterns were then used to align liquid crystals (LCs) in domains measuring several square millimeters.

Porphyrin dye molecules can self-organize on a surface into small columnar stacks of sub-micrometer length (13, 14). These architectures are generated as a result of combined self-assembly and dewetting, which take place simultaneously when a drop-casted solution of the porphyrin molecules is evaporated on a surface. In order to enhance the columnar stacking and hence the length of the assemblies, we have synthesized compound **1** (Fig. 1) (15), which consists of three porphyrin moieties that are linked via amide bonds to a central benzene core, a motif that is known to form extended hydrogen-bonded networks (16–19). Each porphyrin was equipped with three aliphatic hydrocarbon chains to increase the solubility of the stack in organic solvents.

The high tendency of **1** to form aggregates can be directly observed, in that at a concentration of 8 mg/ml, the chloroform solution formed a gel. This strong aggregation is highly dependent on the presence of the alkyl chains, because porphyrin trimers without these chains appeared not to gelate the solvent. In the proton nuclear magnetic resonance (NMR) spectrum of

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